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Technical Field

The present invention relates to a digital watermarking
5 technique and more specifically to a technique that embeds
watermark information in data, such as image data.

Background Art

A variety of digital watermarking techniques have been
10 proposed to embed copyright information in digitalized copies
of images and music. Digitalized data is readily copied in a
complete form (namely, digitalized data has perfect
reproducibility), so that the protecting measure is required
against illegal copies. The digital watermarking technique
15 electronically embeds watermark information, such as
copyright information, in master data in a human-
imperceptible manner. The embedded watermark information can
be taken out according to the requirements. The digital
watermark clearly shows any third party the presence of the
20 copyright in digitalized copies of images and music. The
digital watermark generally includes information for
identifying the copyright holder. The data with the digital
watermark embedded therein may thus be referred to as the
authorized data.

25 The prior art digital watermarking technique, however,
has the drawback that the legal watermark information is not
taken out accurately when another piece of information
overwrites the existing information by a similar procedure.
Alteration to invalidate the digital watermark embedded in
30 the authorized data may hereinafter be referred to as the
overwriting attack against the digital watermark. When the
authorized data is exposed to the overwriting attack to
prevent the embedded legal digital watermark from being
normally read, the digital watermarking loses its

significance. If only an unauthorized watermark is left as the result of the overwriting attack, this allows even the illegal alteration of the signature of the copyright holder.

Electronic data are generally compressed for the purpose of delivery or storage. The digital watermark data embedded by the prior art digital watermarking technique, however, may be altered or even deleted by such data compression. Namely the prior art technique is not sufficiently practical.

Disclosure of the Invention

The object of the present invention is to solve the drawbacks of the prior art technique discussed above and thus to provide an embedding technique that ensures the good preservation of a legal digital watermark and the high secrecy of the digital watermark to any third party even when electronic data open to the public is exposed to overwriting attacks and data compression.

At least part of the above and the other related objects is attained by a method of embedding watermark information in master data. The method includes the steps of: (a) causing the master data to be subjected to discrete Fourier transform; (b) adding a minute variation, which corresponds to a phase difference pattern determined in advance as the watermark information, to either one of a real number array and an imaginary number array of the master data obtained by the discrete Fourier transform, so as to generate resulting data with the minute variation added thereto; and (c) causing the resulting data with the minute variation added thereto to be subjected to inverse Fourier transform, so as to generate authorized data with the watermark information embedded therein.

The present invention is also directed to an apparatus for embedding watermark information in master data, which

corresponds to the above method. The apparatus includes: a transform unit that causes the master data to be subjected to discrete Fourier transform; a phase difference pattern addition unit that adds a minute variation, which corresponds to a phase difference pattern determined in advance as the watermark information, to either one of a real number array and an imaginary number array of the master data obtained by the discrete Fourier transform, so as to generate resulting data with the minute variation added thereto; and an inverse Fourier transform unit that causes the resulting data with the minute variation added thereto to be subjected to inverse Fourier transform, so as to generate authorized data with the watermark information embedded therein.

This technique utilizes the characteristic that a variation of either a real number array or an imaginary number array in a spectrum, which is obtained by discrete Fourier transform of master data in a frequency domain, leads to a variation in phase. The technique of the present invention adds a minute variation corresponding to a phase difference pattern to either the real number array or the imaginary number array obtained by the discrete Fourier transform of the master data and subsequently carries out an inverse transform of the processed data, so as to generate authorized data with watermark information embedded therein. The phase difference pattern is taken out through comparison between the master image data and the authorized data. This arrangement enables the user to intuitively grasp the embedded digital watermark as the phase difference pattern. As long as the master data without the digital watermark embedded therein is not identified, the phase difference pattern can be taken out accurately even after overwriting attacks.

The phase difference pattern is readily written by adding a minute variation ΔF to a spectrum $F(m,n)$ of a

specific frequency (m,n) in either one of the real number array and the imaginary number array obtained by the discrete Fourier transform.

Here it is favorable to carry out the addition of the minute variation ΔF to either the real number array or the imaginary number array while keeping the symmetry of either the real number array or the imaginary number array. As the results of the discrete Fourier transform, the real number array has even symmetry and the imaginary number array has odd symmetry. The addition of the minute variation by considering these points enables good preservation of the intrinsic characteristics of the master data.

The minute variation added as the digital watermark naturally affects the master data. In order to prevent the deteriorating quality of the master data, it is accordingly practical that the minute variation added is within a range of 2 to 10% of the spectrum.

It is also favorable to add the minute variation to a component in a low frequency domain of the real number array or the imaginary number array. In the case of addition to the high frequency component, data compression like JPEG may result in losing the watermark information. In the case of addition to the low frequency domain, on the other hand, data compression does not cause the phase difference pattern as the digital watermark to be lost. The phase difference pattern may, however, be added to the high frequency domain in the case where consideration is given to only reversible compression methods that store the data in the course of compression and restore the original information to a perfect form by expansion of the data.

When there is data with a digital watermark embedded therein according to the method discussed above, that is, when there is authorized data, the method of detecting the watermark information in the authorized data is closely

related to the method of embedding the digital watermark discussed above. These two methods accordingly fulfill the unity condition of the inventions. The present invention is thus directed to a method of detecting watermark information, which includes the steps of: taking out a difference between the master data and the authorized data as a phase difference pattern; and detecting the phase difference pattern as a digital watermark of the authorized data.

This method of detecting the digital watermark adopts the extremely simple technique but is still sufficiently effective. As long as the master data is closed to the public, only the legal owner of the master data can detect the digital watermark. It is extremely difficult to assume the embedded minute variation without the master data.

In order to add the minute variation in such a manner that the digital watermark is not lost by data compression, one applicable method carries out a predetermined data transform to obtain a specific data portion mainly corresponding to a low frequency component from master data, prior to discrete Fourier transform of master data. The method then causes the specific data portion to be subjected to discrete Fourier transform and adds a minute variation corresponding to a predetermined phase difference pattern as watermark information to either one of a real number array or an imaginary number array obtained by the discrete Fourier transform. After the addition of the minute variation, the method carries out inverse Fourier transform and subsequently an inverse transform of the predetermined data transform. The combination of the data compression with the discrete Fourier transform enables the digital watermark to be accurately embedded in the low frequency domain. This method ensures the high resistance against the overwriting attacks, which is discussed above as the effect of the method of embedding the digital watermark by the discrete Fourier

transform, and also effectively prevents the digital watermark data from being altered or deleted by the high degree of data compression. A typical example of the data transform and the inverse data transform is wavelet transform and inverse wavelet transform. Using the wavelet transform and the inverse wavelet transform desirably simplifies the procedures of embedding and restoring watermark information. Any of various known techniques is applicable for the wavelet transform here. A typical example is orthogonal wavelet transform using the Haar basis. Any data transform and inverse data transform other than the wavelet transform and the inverse wavelet transform is also applicable for this method, as long as it follows a transform algorithm to obtain a specific data portion mainly corresponding to the low frequency domain.

When there is authorized data with a digital watermark embedded therein according to the method discussed above, the method of detecting the watermark information is closely related to the method of embedding the digital watermark discussed above. These two methods accordingly fulfill the unity condition of the inventions. The present invention is thus directed to a method of detecting watermark information, which includes the steps of: causing the master data to be subjected to the predetermined data transform of the step (a0); causing the authorized data to be subjected to the predetermined data transform of the step (a0); taking out a difference between the transformed master data and the transformed authorized data as a phase difference pattern; and detecting the phase difference pattern as a digital watermark of the authorized data.

This method of detecting the digital watermark adopts the extremely simple technique but is still sufficiently effective. As long as the master data is closed to the public, only the legal owner of the master data can detect

the digital watermark. It is extremely difficult to assume the embedded minute variation without the master data. For the enhanced safety, it is preferable to conceal the technique applied for the data transform that enables specification of the area mainly corresponding to the low frequency component.

The technique of embedding the digital watermark is applicable for a diversity of data. For example, the master data may be two-dimensional image data. In this case, the phase difference pattern embedded according to the above method is not visually recognizable on the image and causes substantially no deterioration of the picture quality. This technique is also applicable for one-dimensional data, such as sound data.

The embedding method and the embedding apparatus discussed above may be actualized by an application that causes a general-purpose or exclusively used computer to read a storage medium, such as an IC card, a flexible disk, or a CD-ROM, and executes a program stored in the storage medium.

The present invention is thus directed to a storage medium in which a specific program used to embed watermark information in master data is stored in a computer readable manner. The specific program causes a computer to attain the functions of: inputting the master data; causing the input master data to be subjected to discrete Fourier transform; adding a minute variation, which corresponds to a phase difference pattern determined in advance as the watermark information, to either one of a real number array and an imaginary number array of the master data obtained by the discrete Fourier transform, so as to generate resulting data with the minute variation added thereto; and causing the resulting data with the minute variation added thereto to be subjected to inverse Fourier transform, so as to generate authorized data with the watermark information embedded

therein, and outputting the authorized data.

The method of embedding the digital watermark by the combination of the high degree of data compression with the discrete Fourier transform is also actualized by the application that causes the computer to read the storage medium.

The present invention is accordingly directed to a storage medium in which a specific program used to embed watermark information in master data is stored in a computer readable manner. The specific program causes a computer to attain the functions of: inputting the master data; causing the master data to be subjected to a predetermined data transform, which converts the master data to a specific data form that enables an area mainly corresponding to a low frequency component to be specified; causing a specific data portion corresponding to the area out of the converted data to be subjected to discrete Fourier transform; adding a minute variation, which corresponds to a phase difference pattern determined in advance as the watermark information, to either one of a real number array and an imaginary number array of the specific data portion obtained by the discrete Fourier transform, so as to generate resulting data with the minute variation added thereto; causing the resulting data with the minute variation added thereto to be subjected to inverse Fourier transform; and causing the resulting data, which has undergone the inverse Fourier transform, as well as a residual data portion corresponding to a residual area to be subjected to an inverse transform of the predetermined data transform, so as to generate authorized data with the watermark information embedded therein.

The computer generally has the functions of the discrete Fourier transform and the data compression in the form of a library. The function of causing the master data to be subjected to the discrete Fourier transform may thus be

replaced by 'the function of utilizing the computer function that carries out the discrete Fourier transform of the input master data and receiving a real number array or an imaginary number array obtained as a result of the discrete Fourier transform'. In a similar manner, the function of data transform may be replaced by 'the function of utilizing the computer function that converts the input master data into a specific data form, which enables specification of the area mainly corresponding to the low frequency component, and receiving the result of the data transform'.

It is relatively easy to discriminate the overwriting attack against the master data with the digital watermark embedded therein by another technique. The overwriting attack by the same technique is the most serious problem. The effective measure against such an overwriting attack is a method of identifying a phase difference pattern W_1 that is watermark information embedded in master data P_0 , when there is data P_i obtained by embedding other phase difference patterns W_i ($i = 2, 3, \dots$) in authorized data P_1 as watermark information a plurality of times according to the embedding method discussed above, where the authorized data P_1 is obtained by legally embedding the phase difference pattern W_1 in the master data P_0 as the watermark information. The method of identifying the phase difference pattern W_1 as the digital watermark information has thus been developed in relation to the embedding method. Namely the embedding method and the identifying method fulfill the unity condition of the inventions. The identifying method includes the steps of: (d) taking out a difference between the master data P_0 and the data P_i with the other phase difference patterns embedded therein the plurality of times; (e) taking out a difference between the authorized data P_1 and the data P_i with the other phase difference patterns embedded therein the plurality of times; and (f) extracting an eventual difference

between the difference taken out in the step (d) and the difference taken out in the step (e) as the legal phase difference pattern W1.

The present invention is also directed to a method of identifying a phase difference pattern W1 that is watermark information embedded in practical master data Q0, when there is data Qi obtained by embedding other phase difference patterns Wi (i= 2,3,...) in authorized data Q1 as watermark information a plurality of times according to the similar embedding method, where the authorized data Q1 is obtained by converting master data P0 to a specific data form that enables an area mainly consisting of a low frequency component to be specified and then legally embedding the phase difference pattern W1 in the area as the watermark information. The identifying method includes the steps of: (g) taking out a difference between the practical master data Q0 and the data Qi with the other phase difference patterns embedded therein the plurality of times; (h) taking out a difference between the authorized data Q1 and the data Qi with the other phase difference patterns embedded therein the plurality of times; and (i) extracting an eventual difference between the difference taken out in the step (g) and the difference taken out in the step (h) as the legal phase difference pattern W1.

Even when the plurality of overwriting attacks are made, these methods enable extraction of the phase difference pattern legally embedded in the master data and easy identification of the legal data.

The present invention further includes other applications. A first application replaces the Fourier transform with another equivalent transform. Any transform technique is applicable as long as it gives a real number array and an imaginary number array as the result of the transform in a frequency domain. A second application is a

program supply device that supplies a specific computer program, which causes the computer to attain the respective steps or the functions of the respective units discussed above, via a communication path. In this application, programs are stored, for example, in a server on a network and a required program is downloaded to the computer via the communication path and executed to attain the method or the apparatus discussed above. Still another application causes a site (server) located on a network like the Internet to carry out embedding, detection, and identification of the watermark information. In this application, a user who requires embedding, detection, or identification of the watermark information transmits digitalized information like image data to the site on the network, where the process of embedding, detecting, or identifying the watermark information is carried out automatically or manually, and receives the processed data via the network.

Brief Description of the Drawings

Fig. 1 is a block diagram illustrating the structure of a digital watermark processing apparatus in a first embodiment of the present invention;

Fig. 2 is a block diagram showing the functions of a digital watermark embedding unit 42;

Fig. 3 is a flowchart showing a processing routine to embed watermark information executed in the first embodiment;

Fig. 4 shows an example of a master image P0, an image P1 with a digital watermark embedded therein, and an embedded phase difference pattern W01 discussed in the embodiment;

Fig. 5A shows part of a real number array FR of the Fourier transform spectrum obtained in the embodiment;

Fig. 5B shows part of an imaginary number array FI of the Fourier transform spectrum obtained in the embodiment;

Fig. 6 is a flowchart showing the details of the

process of adding the minute variation;

Fig. 7A and 7B show a change of the phase difference pattern of the embodiment due to data compression;

5 Fig. 8A through 8C show changes of the image and the phase difference pattern due to partial replacement of the lower bit plane;

Fig. 9A through 9C show changes of the image and the phase difference pattern due to white noise;

10 Fig. 10 shows the influence of multiple overwriting attacks on the image and the phase difference pattern;

Fig. 11 is a flowchart showing a processing routine to embed watermark information executed in a second embodiment;

Fig. 12A and 12B show the principle of Haar wavelet transform;

15 Fig. 13 shows a process of multi-resolution analysis of the image;

Fig. 14 is a flowchart showing a processing routine to embed watermark information executed in the second embodiment;

20 Fig. 15 shows decomposition to a second level in the second embodiment;

Fig. 16A shows a resulting image with a watermark embedded therein;

25 Fig 16B shows a resulting phase difference pattern obtained in the second embodiment;

Fig. 17A through 17I show the influence of multiple overwriting attacks on the resulting image with the watermark embedded therein;

30 Fig 17J shows the difference $|S1a - S1b|$ between the frequency spectra $F1a$ and $F1b$;

Fig. 18A through 18C show results of evaluation of the picture quality by embedding of watermark;

Fig. 19A through 19F show results of evaluation of the resistance against JPEG compression;

Fig. 20A through 20F show results of evaluation of the resistance against deletion of the lower bit plane;

Fig. 21A through 21F show results of evaluation of the resistance against addition of noise; and

5 Fig. 22A through 22F show results of evaluation of resistance against tone conversion.

Best Modes of Carrying Out the Invention

A. General Structure of Apparatus

10 Some modes of carrying out the present invention are discussed below as preferred embodiments. Fig. 1 is a block diagram illustrating the structure of a digital watermark processing apparatus 10 in one embodiment of the present invention. The digital watermark processing apparatus 10 is
15 a computer including a CPU 22, a main memory 24 including a ROM and a RAM, a frame memory 26, a keyboard 30, a mouse 32, a display unit 34, a hard disk 36, a modem 38, a scanner 39 that reads images, and a bus 40 that connects the preceding constituents with one another. A diversity of interface
20 circuits are omitted from the illustration of Fig. 1. The modem 28 is connected to a computer network NT via a non-illustrated communication line. A server SV on the computer network NT functions as a program supply device that supplies any required computer program to the digital watermark
25 processing apparatus 10 via the communication line.

A computer program is stored in the main memory 24 to attain the functions of a digital watermark embedding unit 42. The functions of the digital watermark embedding unit 42 will be discussed later.

30 The computer program that attains the functions of the digital watermark embedding unit 42 is provided in a specific form recorded in a computer readable recording medium, such as a flexible disk or a CD-ROM. The computer reads the computer program from the recording medium and transfers the

computer program to either an internal storage device or an external storage device. Alternatively the computer program may be supplied to the computer via the communication path. A microprocessor included in the computer executes the computer program stored in the internal storage device to attain the functions specified by the computer program. In accordance with an alternative procedure, the computer reads the computer program recorded in the recording medium and directly executes the computer program.

In the specification hereof, the term 'computer' expresses the concept including a hardware device and an operating system and thus represents the hardware device working under the control of the operating system. In the case where the operating system is not required but an application program alone can activate the hardware device, the hardware device itself is equivalent to the computer. The hardware device includes at least a microprocessor like a CPU and means for reading the computer program recorded in the recording medium. The computer program includes program codes that cause the computer to attain the functions of the respective units discussed previously. Part of the functions may be attained not by the application program but by the operating system.

Typical examples of the 'recording medium' adopted in the present invention include flexible disks, CD-ROMs, magneto-optic discs, IC cards, ROM cartridges, punched cards, prints with barcodes or other codes printed thereon, internal storage devices (memories like a RAM and a ROM) and external storage devices of the computer, and a variety of other computer readable media.

First Embodiment

B. Process of Embedding Watermark Information 1:

Fig. 2 is a block diagram illustrating the functions of

the digital watermark embedding unit 42 that regulates the phase of either a real number array and an imaginary number array obtained by discrete Fourier transform and thereby embeds watermark information. The digital watermark

embedding unit 42 includes a discrete Fourier transform unit 50, a minute variation addition unit 52, and an inverse Fourier transform unit 54. These units respectively correspond to the transform unit, the phase difference pattern addition unit, and the inverse Fourier transform unit of the present invention.

The functions of the respective units are described briefly. The discrete Fourier transform unit 50 causes image data read by the scanner 39 to undergo discrete Fourier transform. Discrete Fourier transform F of an image P_0 , which includes M pixels in the horizontal direction and N pixels in the vertical direction, is expressed by Equation (1) given below, when $p(m,n)$ denotes a pixel value of the image P_0 . Here $m= 0, 1, \dots, M-1$ and $n= 0, 1, \dots, N-1$.

$$F(u,v) = \frac{1}{MN} \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} p(m,n)W$$

$$W = e^{-j2\pi(mu/M + nv/N)} \quad (1)$$

where $j = \sqrt{-1}$.

The matrix F obtained by the discrete Fourier transform (the Fourier spectrum) represents the spatial frequency component of the image P_0 . Since $\exp(-j\theta) = \cos\theta \pm j\sin\theta$ according to the Euler's formula, a real number array $FR(u,v)$ of the above matrix F has even symmetry and an imaginary number array $FI(u,v)$ has odd symmetry. The relationships expressed by Equations (2) given below hold with regard to $F(\pm u, \pm v)$ where $u= 0, 1, 2, \dots, M-1$ and $v = 0, 1, 2, \dots, N-1$:

$$\begin{aligned} F(u, -v) &= F(u, N-v); \\ F(-u, v) &= F(M-u, v); \text{ and} \\ F(-u, -v) &= F(M-u, N-v). \end{aligned} \quad (2)$$

Further extension by noting the periodicity of the above matrix gives the equation of:

$$F(aM+u, bN+v) = F(u, v)$$

where both a and b denote integers.

5 The minute variation addition unit 52 embeds the phase difference pattern as the digital watermark in the matrix F obtained by the discrete Fourier transform unit 50. The actual procedure of embedding the phase difference pattern will be discussed later. A minute deviation is added to the
10 predetermined spectrum of the matrix, in order to keep the symmetry of the matrix obtained by the Fourier transform.

 The inverse Fourier transform unit 54 causes the resulting data with the phase difference pattern embedded therein as the digital watermark to be subjected to an
15 inverse transform of the discrete Fourier transform carried out by the discrete Fourier transform unit 50. The inverse transform is expressed by Equation (3) given below, based on the expression of Equation (1):

$$p(m, n) = \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} F(u, v) W^{-1} \quad (3)$$

20 Here an inversely transformed pixel value $p(m, n)$ also has the symmetry discussed above and holds the relationship of:

$$p(aM+m, bN+n) = p(m, n)$$

25 The following describes the technique of embedding the digital watermark in this embodiment, especially a series of the processing carried out by the minute variation addition unit 52, with referring to the flowchart of Fig. 3. The flowchart of Fig. 3 shows a processing routine executed by
30 the CPU 22 to embed a digital watermark. When the program enters the digital watermark embedding routine, the CPU 22 first reads the image P0 (step S100). This process may be attained by driving the scanner 39 to directly read image

data from a photograph or another original or by reading an image file provided in advance. In the latter case, the image file may be stored in, for example, a CD-ROM or alternatively be transmitted by communications via the modem

5 38. Fig. 4A shows an example of the input image P0. This input image P0 consists of 256×256 pixels, where each pixel has a tone value in the range of 256 tones (8 bits).

The CPU 22 then causes the input image data to undergo discrete Fourier transform (step S110). The discrete Fourier transform is carried out as the operations by the discrete Fourier transform unit 50 as discussed above. The discrete Fourier transform unit 50 may be actualized by an exclusive processor or as operations by the CPU 22. The process of carrying out the discrete Fourier transform (DFT) is provided
10 in the form of a library as well known in the art and is not specifically described here.
15

The discrete Fourier transform gives the matrix $F(u,v)$. Part of the matrix F thus obtained is shown in Fig. 5. As a matter of convenience, Fig. 5 shows only the part relating to elements $u,v = 0,1,2,3$ and $u,v = 253, 254, \text{ and } 255$. Fig. 5A shows the coefficients of the real number array FR , and Fig. 5B shows the coefficients of the imaginary number array FI . For better understanding of the symmetry discussed above, the element $(0,0)$ is on the center of the arrays in Figs. 5A and 5B. The CPU 22 subsequently adds a minute variation to the matrix F (step S120), causes the matrix F with the minute variation added thereto to undergo an inverse transform (step S130), and outputs the result of the inverse transform as image data with the digital watermark embedded therein (step
20 S140). A resulting image P1 with the digital watermark embedded therein is shown in Fig. 4B.
25
30

The process of adding the minute variation (step S120) is described in detail with referring to the flowchart of Fig. 6. A minute variation ΔF is added to either the real

number array FR or the imaginary number array FI. The following description regards the addition to the imaginary number array FI. The addition to the real number array FR follows a similar procedure with a difference in symmetry.

5 The procedure first specifies elements of interest, to which the minute variation ΔF is added (step S122). In the case of the addition of the minute variation ΔF in a high frequency domain or in the case of the sufficiently small magnitude of the minute variation ΔF , the minute variation ΔF added is
10 visually unrecognizable on the resulting image obtained by the inverse transform. There is, however, some possibility that the minute variation added in the high frequency domain is lost by data compression. For the enhanced resistance against data compression, the procedure of this embodiment
15 adds the minute variation ΔF , which has the restricted magnitude of not greater than a predetermined level, in a low frequency domain. Namely the elements of interest specified for the addition of the minute variation ΔF are restricted to the low frequency domain. In a concrete example, the
20 procedure specifies elements FI(0,2) and FI(2,0) for the addition of the minute variation ΔF ($=1.0 \times 10^4$). According to Equations (2) representing the symmetry of the matrix F, the procedure also specifies elements FI(0,254) and FI(254,0) for subtraction of the minute variation ΔF . As discussed later,
25 the eventual shape of the phase difference pattern as the digital watermark depends on the elements specified for addition of the minute variation ΔF and on the magnitude of the minute variation ΔF . The specification of the elements for addition of the minute variation is thus directly
30 connected to the digital watermarking (the signature). The procedure of this embodiment accordingly does not fix the elements to which the minute variation ΔF is added nor the magnitude of the minute variation ΔF .

The procedure then specifies the magnitude of the minute variation ΔF (step S124). As described above, the magnitude of the minute variation ΔF affects the picture quality of the resulting image with the digital watermark embedded therein. A certain restriction is thus placed on the magnitude of the minute variation ΔF . The procedure of the embodiment regulates the magnitude of the minute variation ΔF to be within a range of 2 to 10% of the specified elements. In the concrete example, the procedure specifies the magnitude of the minute variation to approximately 5% of the elements.

The procedure adds the minute variation ΔF of the magnitude specified at step S124 to the elements specified at step S122 (step S126). In the concrete example, the procedure adds the minute variation $\Delta F = 1.0 \times 10^4$ to the elements $FI(0,2)$ and $FI(2,0)$ and subtracts the same value ΔF from the elements $FI(0,254)$ and $FI(254,0)$.

After completion of the addition of the minute variation, the inverse Fourier transform is carried out as shown in the flowchart of Fig. 3. The resulting image $P1$ (see Fig. 4B) obtained by the inverse Fourier transform is expressed by Equation (4) given below:

$$P1 = \{p1(m,n) | m,n = 1, 2, \dots, 255\} \quad (4)$$

In the processed image $P1$, only the imaginary number component is varied at its spatial frequency; that is, only the phase varies. The resulting image $P1$ is accordingly changed from the master image $P0$ by a phase component $\Delta\theta$ corresponding to the minute variation ΔF added. The difference between the pixel values p of these two images gives a phase difference $W01$. The phase difference $W01$ is defined by Equation (5) given below:

$$W01 = \{w01(m,n) | m,n = 1, 2, \dots, 255\}$$

$$\text{where } w01(m,n) = p0(m,n) - p1(m,n) \quad (5)$$

The absolute value $|W01|$ of the phase difference $W01$ in Equation (5) is determined and illustrated as the pattern of Fig. 4C in this embodiment. This pattern is called the phase difference pattern. The phase difference pattern $W01$ depends upon the coordinate values (u,v) of the elements specified for the addition of the minute variation ΔF and the magnitude of the minute variation ΔF added. The phase difference pattern $|W01|$ is accordingly regarded as the digital watermark. Varying the combination of:

(1) the selection of the elements to which the minute variation ΔF is added; with

(2) the magnitude of the minute variation ΔF added to the elements ensures numerous variations of the phase difference pattern. The phase difference pattern is accordingly used as the electronic signature. The phase difference pattern used as the signature has a characteristic shape including a two-dimensional repetition as shown in Fig. 4C and is readily recognized by the human as a graphical pattern. The master image $P0$ in which the digital watermark is embedded should be closed to the public.

The digital watermark embedding apparatus and the corresponding method are described above as one embodiment of the present invention. Several conditions are required for the functions of the embedded data as the digital watermark. One of the conditions is the resistance against the noise occurring, for example, due to data compression as described previously. The embedding method of the embodiment adds the minute variation ΔF in the low frequency domain, so that the embedded data has sufficiently high resistance against a certain type of data compression that deletes information in a high frequency domain. The noise resistance is described in detail with some examples.

The discussion first regards the resistance against data compression. Here the digital watermark is embedded in the master image P0 according to the procedure discussed above. The procedure adds the minute variation ΔF corresponding to the phase difference pattern W01 to the Fourier spectrum of the master image P0 and carries out the inverse transform to obtain the image P1. The resulting image P1 is compressed to 75% by the JPEG technique. The data compression loses part of the information included in the master image and causes some noise. Fig. 7 shows an example of such cases. In the example of Fig. 7, the phase difference pattern |W01| (see Fig. 7A) embedded in the image P1 is changed to a phase difference pattern |W01'| (see Fig. 7B) extracted from a compressed image P1'. Regardless of the relatively high superposing noise, the shape of the phase difference pattern is not destroyed significantly. The phase difference pattern can thus be still used as the signature.

The description then regards the resistance of the digital watermark of the embodiment against deletion of a lower bit plane. Fig. 8A shows the phase difference pattern embedded in the master image P0. Data with regard to a lower bit plane 0 to 2 are deleted from the authorized image P1 and replaced by the value '0'. Fig. 8B shows a resulting image P1' thus obtained. Replacement of the data in the lower bit plane 0 to 2 with the value '0' causes some noise. A phase difference pattern |W01'| extracted as the difference between the resulting image P1' and the master image P0 still has the characteristic of the embedded phase difference pattern as shown in Fig. 8C and thus functions as the digital watermark.

The discussion subsequently regards the resistance against white noise in the range of -40 dB to +40 dB applied to the image with the phase difference pattern embedded therein as the digital watermark. Fig. 9B shows a resulting image P1' with white noise added after embedding of the phase

difference pattern $|W01|$ shown in Fig. 9A. A phase difference pattern $|W01'|$ extracted as the difference between the resulting image $P1'$ and the master image $P0$ well keeps the characteristic of the embedded phase difference pattern as shown in Fig. 9C. The digital watermarking of the embodiment sufficiently functions even in the case of superposing white noise.

The above description shows the high resistance of the digital watermark of the embodiment against the diversity of noises. Other conditions required for the digital watermark are that only the person accepting the legal permission can take the digital watermark out of the image and that the watermark information can not be deleted or altered by any illegal technique. These points are described in detail below.

In this embodiment, the master image $P0$ is closed to the public, while the processed image $P1$ with the digital watermark embedded therein is open to the public. It is accordingly required that the watermark information can not be read without the permission from the processed image $P1$ with the digital watermark embedded therein. The image $P1$ with the digital watermark embedded therein consists of the master image $P0$ and the minute variation ΔF added to the Fourier spectrum of the master image $P0$. As long as the master image $P0$ is concealed, it is impossible for any third party to take the phase difference pattern $|W01|$ functioning as the signature out of the authorized image $P1$.

Even when the Fourier spectrum is obtained by the Fourier transform of the authorized image $P1$, the watermarking of the embodiment does not allow specification of the magnitude of the minute variation ΔF and the elements $F(u,v)$ to which the minute variation ΔF is added. The magnitude of the minute variation ΔF required for separation

of the phase difference pattern $|W01|$ is only several percent of the values of the elements. The minute variation ΔF is thus not conspicuous in the Fourier spectrum. The arrangement of the embodiment accordingly does not allow the minute variation added to some elements to be estimated from the values of the elements having a variation of only about 5%.

The discussion regards the resistance of the digital watermark against the overwriting attacks. A variety of techniques are applicable for the overwriting attacks against the digital watermark. One of the most heavily affecting techniques is the overwriting attacks according to the same algorithm. It is impossible to illegally identify or even estimate the magnitude of the minute variation ΔF or the elements $F(u,v)$ to which the minute variation ΔF is added, from the authorized image $P1$. It is thus virtually impossible that the minute variation is illegally added under the identical conditions. There is, however, still some possibility that the person who understands the concept of the phase difference pattern tries to make overwriting attacks according to the same algorithm. Here it is thus assumed that the authorized image $P1$ is exposed to at least one overwriting attack. The person who makes an i -th overwriting attack (hereinafter referred to as the i -th forger) assumes an available image P_{i-1} as the master image, embeds the phase difference pattern in the image P_{i-1} , and makes a resulting image P_i open to the public, and claims that the image P_i is the authorized image. In this case, the i -th forger claims the difference between the two images $W_{i-1,i} = P_{i-1} - P_i$ ($i = 2, 3, \dots$) as the legal watermarking pattern.

The legal owner of the image $P0$ (that is, the legal signatory) readily obtains the phase differences $W0i = P0 - P_i$ and $W1i = P1 - P_i$, based on the image $P1$ open to the public by

the legal signatory and the image P_i open to the public by the i -th forger. The eventual difference between these phase differences W_{0i} and W_{1i} is given as:

$$\Delta W = W_{0i} - W_{1i} = (P_0 - P_i) - (P_1 - P_i) = P_0 - P_1 = W_{01}$$

5 The legal owner of the image P_0 can thus readily take the own signature W_{01} from the forged image P_i open to the public P_i . This means that the legal signature is still kept in the forged image P_i even when the image P_1 open to the public is exposed to multiple overwriting attacks.

10 Figs. 10 shows an example of the above description in the case of $i=2$. The phase difference pattern $|W_{01}|$ of Fig. 10 (d) is added as the legal signature to the master image P_0 shown in Fig. 10 (a) by a process S_1 . It is here assumed that the forgery carries out a process S_2 to add another
15 phase difference pattern to the legally processed image P_1 (see Fig. 10 (b)) obtained by the process S_1 and makes an illegally processed image P_2 shown in Fig. 10(c) open to the public. In this case, a phase difference pattern $|W_{02}|$ shown in Fig. 10 (e) is obtained as the difference between the
20 illegally processed image P_2 open to the public and the master image P_0 . In a similar manner, a phase difference pattern $|W_{12}|$ shown in Fig. 10 (f) is obtained as the difference between the legally processed image open to the public by the legal owner and the master image P_0 . The
25 eventual difference between these two differences is obtained as a phase difference pattern shown in Fig. 10 (g). This perfectly coincides with the signature that the legal owner adds to the master image. In this example, $i=2$, so that the phase difference pattern W_{12} added by the forger is
30 identified. As in the case of $i=3$, however, it is not necessary to know the phase difference pattern added by the forger. Even when the phase difference pattern added by the forger is unknown, this arrangement of the embodiment enables the phase difference pattern embedded by the legal owner to

be accurately taken out of the image that has been exposed to plural overwriting attacks.

As described above, the digital watermark embedded by the method of the embodiment has sufficient resistance against the data compression as well as the plural overwriting attacks. Even in the combination of the overwriting attacks with the noise or data compression discussed above with reference to Figs. 7 through 9, the phase difference pattern added to the mater image P0 is well preserved and used as the digital watermark.

Second Embodiment

C. Process of Embedding Watermark Information 2

Fig. 11 is a functional block diagram showing the functions of the digital watermark embedding unit 42 in another embodiment. The digital watermark embedding unit 42 of this embodiment embeds the watermark information through a combination of a data compressing process with a process of regulating the phase of either a real number array or an imaginary number array of the Fourier transform. The series of the processing excluding the process relating to the data compression is identical with that executed in the first embodiment. The following description accordingly concentrates on the characteristic part of the second embodiment.

The digital watermark embedding unit 42 includes a data compression unit 60 and a data decompression (expansion) unit 68, in addition to a discrete Fourier transform unit 62, a minute variation addition unit 64, and an inverse Fourier transform unit 66 that are identical with the corresponding elements of the first embodiment. The data compression unit 60 and the data decompression (expansion) unit 68 respectively correspond to the data transform unit and the inverse transform unit of the present invention.

The functions characteristic of this embodiment are described briefly. The data compression unit 60 causes the image data read by the scanner 39 to undergo wavelet transform. Refer to 'Wavelet Beginner's Guide' (Tokyo Denki University Press 1995) for the details of the wavelet transform. The procedure of this embodiment applies the simplest orthogonal wavelet transform using the Haar basis.

A transform of Equation (6) is defined with regard to an area of 2 by 2 pixels shown in Fig. 12A:

$$\begin{bmatrix} \omega 0 \\ \omega 1 \\ \omega 2 \\ \omega 3 \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{bmatrix} \begin{bmatrix} I0 \\ I1 \\ I2 \\ I3 \end{bmatrix} \quad (6)$$

The results of the transform are shown in Fig. 12B. The method of applying this operation rule successively to 1/2x1/2 areas over the whole range of a given image according to the procedure shown in Fig. 13 is called the Haar wavelet transform. The decomposition is reflexively repeated n times until each portion LLn consists of 1x1 pixel. When a master image is halved both in the vertical direction and in the horizontal direction, LL1, LH1, HL1, and HH1 on the first level respectively represent a direct current component, a difference in the horizontal direction, a difference in the vertical direction, and a difference in the diagonal direction. LL denotes a multi-resolution approximation (hereinafter referred to as the MRA component), whereas LH, HH, and HL denote multi-resolution representations (hereinafter referred to as the MRR components). Namely the portion LL has the low frequency component of the image, and the other portions have the high frequency component of the image.

The general data compression technique typically

follows an algorithm that deletes the high frequency component of the image. In the case where watermark information is embedded in the high frequency domain of the image, the watermark information may be lost in the process of compressing the image.

The prior to the Fourier transform discussed in the first embodiment, the procedure of the second embodiment carries out the wavelet transform of master image data and causes the multi-resolution approximation (MRA) component, which affluently keeps luminance information of the master image, to undergo the Fourier transform, so as to embed the watermark information as the phase difference pattern. This arrangement ensures the synergistic effects, that is, the heightened resistance against the data compression, which is relatively low in the case of embedding of the phase difference pattern by the Fourier transform alone, and easy discrimination of the overwriting attacks, which are not prevented by the wavelet transform alone.

After the processing of the data compression unit 60, the procedure embeds the phase difference pattern through the series of the processing carried out by the discrete Fourier transform unit 62, the minute variation addition unit 64, and the inverse Fourier transform unit 66 in the same manner as the first embodiment, and eventually activates the data decompression (expansion) unit 68 to carry out the inverse wavelet transform. This gives image data with the digital watermark embedded therein.

The following describes the procedure of embedding the digital watermark in the second embodiment with referring to the flowchart of Fig. 14. The flowchart of Fig. 14 shows a processing routine executed by the CPU 22 to embed a digital watermark. When the program enters the digital watermark embedding routine, the CPU 22 first reads a master image P0 (step S200) and causes the input image data to undergo the

wavelet transform (step S210). Fig. 15 shows resulting image data obtained by decomposition of the master image data P0 shown in Fig. 4A to the second level. An area LL2 encircled by the broken line denotes the MRA component. As clearly understood from Equation (6) discussed above, this area is substantially equal to the down sampled standard data and mainly consists of the low frequency component.

The CPU 22 subsequently causes the image data in the area LL2 to undergo the discrete Fourier transform (step S220) and adds $\Delta FI(0,2) = \Delta FI(2,0) = 1.0 \times 10^2$ as a watermark signal S1 to the coordinate values (0,2) and (2,0) of the imaginary number array FI obtained by the discrete Fourier transform (step S230). In order to keep the symmetry, at the same time, $\Delta FI(0,62) = \Delta FI(62,0) = -1.0 \times 10^2$ is added to the coordinate values (0,62) and (62,0).

The CPU 22 then carries out the inverse Fourier transform (step S240), causes the whole range of the image shown in Fig. 15 to undergo the inverse wavelet transform to the upper-most level (step S250), and outputs a final resulting image with the digital watermark information embedded therein (step S260). The series of processing gives a processed image Q1 ($=\{q1(m,n) | m,n = 0, 1, 2, \dots, 255\}$), which is changed from the master image P0 by a phase component $\Delta\theta$ corresponding to the minute variation ΔFI as shown in Fig. 16A. The addition of the digital watermark information causes substantially no deterioration of the picture quality of the resulting image Q1, compared with the master image P0. Even when the processed image Q1 is exposed to irreversible data compression that deletes the high frequency component, the digital watermark embedded in the area LL2 corresponding to the low frequency component is not lost.

Like the first embodiment, the digital watermark added as the phase difference pattern is defined by a difference

between the pixel values of the two images $\{P0, Q1\}$, that is, by a phase difference $W01$ as discussed below. The inverse wavelet transform of the image $LL2$ shown in Fig. 15 to the upper-most level without any embedding process gives an image
5 $Q0$ ($=\{q0(m,n) | m,n= 0, 1, 2, \dots, 255\}$). Here $Q0$ is approximately equal to $P0$. The absolute value $|W01|$ of the phase difference $W01$ between the image $Q0$ and the processed image $Q1$ is determined and illustrated as the phase difference pattern of Fig. 16B. This phase difference
10 pattern is used as the digital watermark.

In this embodiment, the master image $P0$ is required for extraction of the phase difference pattern. As long as the master image $P0$ is closed to the public, any third party can not extract the digital watermark information only from the
15 processed image $Q1$. As discussed in the first embodiment, it is virtually impossible to estimate $\Delta FI(u,v)$ from the processed image $Q1$.

The digital watermarking of this embodiment also has the sufficient resistance against the overwriting attacks by
20 the same algorithm. The i -th forger regards an available image $Qi-1$ as the master image, carries out the wavelet transform of the image $Qi-1$, adds the watermark signal Si according to the same algorithm, and carries out the inverse wavelet transform to generate a resulting image Qi . The i -th
25 forger makes the image Qi open to the public and claims the difference between the two images $Wi-1= Qi-1 - Qi$ as the legal watermarking pattern.

The legal owner of the image $P0$ (that is, the legal signatory) readily obtains the phase differences $W0i= Q0 - Qi$
30 and $W1i= Q1 - Qi$, based on the image $Q1$ open to the public by the legal signatory and the image Qi open to the public by the i -th forger. The legal owner of the image $Q0$ ($\approx P0$) can prove that an eventual difference $W01$ has been embedded in the image Qi open to the public. The eventual difference is

given as:

$$W0i - W1i = (Q0 - Qi) - (Q1 - Qi) = Q0 - Q1 = W01 \quad (7)$$

The legal owner of the image $Q0$ can thus readily take the own signature $W01$ from the forged image Qi open to the public.

5 Figs. 17A through 17(g) show an example of the above description in the case of $i=2$. Addition of the watermark signal $S1$ to the practical master image $Q0$ shown in Fig. 17A gives a legal processed image $Q1$. The difference between the images $Q0$ and $Q1$ defines the phase difference pattern of Fig. 10 17D. Even when the image $Q1$ is illegally overwritten by another watermark signal $S2$, the legal phase difference pattern is still kept in an illegally processed image $Q2$ as shown in Fig. 17(g).

15 Conspiratorial attacks are the severer version of the overwriting attacks. When the legal owner of the master image $P0$ delivers copies of the master image $P0$ (with different pieces of digital watermark information embedded therein) to two or more people, it is possible to estimate the master image $P0$ by the conspiracy of the receivers. In 20 some forms of delivery, different signatures or digital watermarks are required for an identical image. For example, it is assumed that illegal copies are found after legal copies of one identical image are delivered to two or more people. In order to identify the source of the illegal 25 copies, it is required to embed different signatures in the legal copies of the image. It is accordingly desirable to add different signatures to the image when plural copies are legally delivered to different channels. When there are two or more copies of the identical image with different digital 30 watermarks embedded therein by the same algorithm, it becomes easier to illegally identify the digital watermarks embedded in the plurality of legal copies even if the master image is closed to the public.

The following briefly describes the resistance of the

digital watermarking of the embodiment against such conspiracy attacks. For the purpose of simplicity of discussion, it is assumed that processed copies Q1a and Q1b of an identical master image with different watermark signals S1a and S1b embedded therein are respectively delivered to receivers a and b. The watermark signals S1a and S1b are identified by calculating the difference between frequency spectra F1a and F1b obtained by the Fourier transform of the copies Q1a and Q1b. When S1a is not equal to S1b, a Fourier spectrum F0 of the master image is estimated from the result of $F(S1a, S1b)$ and the Fourier spectra F1a and F1b. The inverse conversion of the estimated Fourier spectrum F0 reconstructs an image Q0 approximate to the master image P0. This results in estimating a watermark signal S1. The effective countermeasure against such conspiratorial attacks compresses the processed copies of the master image with the minute variation ΔF embedded therein at different compression rates to distort the distributions of the frequency spectra F1a and F1b. Another effective countermeasure adds the minute variations ΔF of different absolute values at an identical position on the Fourier spectra. An example of the latter countermeasure is shown in Figs. 17H through 17J. Fig. 17H shows an image obtained by embedding watermark signals S3 of different quantities at an identical position on the frequency spectra F1a and F1b. Fig. 17I shows the phase difference pattern corresponding to the watermark signal S3. In this example, the difference $|S1a - S1b|$ between the frequency spectra F1a and F1b shown in Fig. 17J appears as a value accumulated at the identical position. It is practically impossible to estimate the values of spectra corresponding to the digital watermarks respectively added to the two copies of the master image.

The arrangement of the embodiment has advantages over other arrangements of image processing. Figs. 18A through

18C show the mapping of phase difference patterns to resulting output images with a change of the value of the minute variation $\Delta F1(u,v)$, which is required to generate a processed image Q1 with the digital watermark embedded therein. This clearly shows that the increasing quantity of the embedded information deteriorates the picture quality and disturbs the image expression. Substantially no visual deterioration is, however, observed in the output image at the quantity of the embedded information up to $\Delta F1(u,v) = 2.0$. The quantity of the embedded information in this range is thus sufficiently practical.

Fig. 19 shows the results of an experiment with regard to the data compression and the overwriting attacks. Fig. 19A shows the phase difference pattern $|W01|$ of the processed image Q1 with the digital watermark embedded therein according to the technique of the second embodiment. Fig. 19B shows a resulting image Q'1 when the processed image Q1 is compressed to 75% by the JPEG method. This image Q'1 includes some noise corresponding to the difference from a non-compressed master image Q0 ($\approx P0$). In this state, the phase difference pattern W01 is changed to $W'01 = Q0 - Q'1$ as shown in Fig. 19C. When a third party embeds a phase difference pattern $W''12 (= Q'1 - Q'2)$ shown in Fig. 19D in the image Q'1, the phase difference pattern of the image is changed to $W'02$ as shown in Fig. 19E. In this case, the phase difference pattern W01 is extracted according to the following relation:

$$W'02 - W'12 = W'01 \approx W01 \quad (8)$$

using a phase difference pattern $W'12$ (see Fig. 19F) obtained as the difference between the images Q1 and Q2.

Fig. 20 shows the resistance of the digital watermarking of the second embodiment against deletion of the lower bit plane. Fig. 20A shows the phase difference pattern

|W01| added as the digital watermark. Data with regard to the lower bit plane of 0 to 1 in the image Q1 with the watermark signal S1 embedded therein are deleted and replaced with the value '0'. The image is then subjected to the normalization process to have the maximum value of 255. Fig. 20B shows an image Q'1 thus obtained. The deletion of the lower bit plane causes the difference between the image Q'1 and the master image P0 to have some noise, and the phase difference pattern W01 is changed to a phase difference pattern W'01 shown in Fig. 20C. When a third party embeds a phase difference pattern W''12 (= Q'1 - Q'2) shown in Fig. 20D as a new digital watermark in the image Q'1, the phase difference pattern is changed to W'02 as shown in Fig. 20E. In this case, a pattern substantially identical with the legal phase difference pattern W01 is extracted according to Relation (8) given above using a phase difference pattern W'12 shown in Fig. 20F. The results of the experiment with the varying range of the lower bit plane to be deleted show that the phase difference pattern can be restored as long as the range of deletion of the lower bit plane is 0 to 3.

The following description regards the preservation of the watermark when a variety of noises are applied to the processed image with the digital watermark embedded therein. Fig. 21 shows the results of the experiment that applies Gaussian noise in the range of -40 dB to + 40 dB to the image Q1 with the phase difference pattern W01 shown in Fig. 21A as the digital watermark signal S1. Fig. 21B shows a resulting image Q'1 with noise. In this case, the difference between the image Q'1 and the master image P0 causes noise, and the embedded phase difference pattern W01 is changed to a pattern W'01 as shown in Fig. 21C. When a third party embeds a phase difference pattern W''12 (= Q'1 - Q'2) shown in Fig. 21D as a new digital watermark in the image Q'1 with noise, the phase difference pattern is changed to W'02 as shown in Fig. 21E.

In this case, a pattern substantially identical with the phase difference pattern W01 corresponding to the legal digital watermark is extracted according to Relation (8) given above using a phase difference pattern W'12 (see Fig. 21F). Namely the digital watermarking of the embodiment has sufficient resistance against such superposition of noise.

Fig. 22 shows the results of the experiment with tone conversion according to the error diffusion method. Fig. 22(a) shows the phase difference pattern $|W01|$. Fig. 22B shows the result of the processing that converts the image Q1 with the phase difference pattern W01 embedded therein as the watermark signal S1 to have only 6 tones. The tone reduction results in the image Q'1. The difference between the image Q'1 and the master image P0 causes some noise, and the embedded phase difference pattern W01 is changed to a phase difference pattern W'01 shown in Fig. 22C. When a third party embeds a phase difference pattern W''12 ($= Q'1 - Q'2$) shown in Fig. 22D as a new digital watermark in the image Q'1, the phase difference pattern is changed to W'02 as shown in Fig. 22E. In this case, a pattern substantially identical with the phase difference pattern W01 corresponding to the legal digital watermark is extracted according to Relation (8) given above using a phase difference pattern W'12 shown in Fig. 22F.

As described above, the digital watermark embedded by the method of the second embodiment has sufficient resistance against the data compression as well as the plural overwriting attacks, and ensures practical resistance against the most malicious conspiratorial attacks. Even in the combination of the overwriting attacks with the noise or data compression discussed above with reference to Figs. 19 through 22, the phase difference pattern added to the master image P0 is well preserved and used as the digital watermark.

The present invention is not restricted to the above

embodiments or their modifications, but there may be many other modifications, changes, and alterations without departing from the scope or spirit of the main characteristics of the present invention. For example, one
5 modified procedure adds the minute variation to the real number array of the matrix obtained by the Fourier transform. Another modified procedure adds the minute variation to the elements corresponding to a high frequency domain of the matrix obtained by the Fourier transform. The data transform
10 for specifying the area mainly consisting of the low frequency component is not restricted to the wavelet transform, but may be carried out by any other suitable method. Here the wavelet transform is not limited to the Haar wavelet transform but includes the wavelet transform
15 according to another basis or technique.

Industrial Applicability

The technique of the present invention is applicable for apparatuses of embedding watermark information in
20 electronic data and apparatuses of electronic identification. The technique is effectively applied for embedding copyright information, for personal identification in the case of electronic transactions, and for cryptography that includes apparatuses and methods of encryption, transmission, and
25 decryption.